#### 21UMAC400 Engineering Mathematics-IV

(2-2-0)3

Contact Hours:39 CIE:50 Marks SEE: 50 Marks Exam Duration:3 Hrs.

#### **Course Learning Objectives (CLOs):**

To provide an insight into applications of conformal mapping, integration of complex functions and application of statistics and probability distributions in Engineering.

Course Outcomes (COs):

| Descr          | iption of the Course Outcome:  | Mapping to POs(1-12)         |                       |                     |  |  |  |  |  |  |
|----------------|--|------------------------------|-----------------------|---------------------|--|--|--|--|--|--|
| At the able to | end of the course the student will be  | Substantia<br>I<br>Level (3) | Moderate<br>Level (2) | Slight<br>Level (1) |  |  |  |  |  |  |
| CO-1           | <b>Construct</b> and use the concepts of analytic function to solve the problems arising in Engineering field.                       |                              |                       | 1                   |  |  |  |  |  |  |
| CO-2           | <b>Utilize</b> conformal transformation<br>and complex integral to transform<br>irregular domain onto a relatively<br>simple domain. |                              | 1                     |                     |  |  |  |  |  |  |
| CO-3           | <b>Make</b> use of the correlation and regression analysis tofit a suitable mathematical model for the statistical data.             |                              | 1,2                   |                     |  |  |  |  |  |  |
| CO-4           | <b>Apply</b> discrete and continuous probability distributions in analyzing the probability models arisingin engineeringfield.       |                              | 1,2                   |                     |  |  |  |  |  |  |
| CO-5           | <b>Recite</b> Markov chains and describe stochastic process.   |                              |                       | 1,2                 |  |  |  |  |  |  |
| DOa            |  |                              | 0 40 44               | 40                  |  |  |  |  |  |  |

| POs           | 1   | 2   | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|---------------|-----|-----|---|---|---|---|---|---|---|----|----|----|
| Mapping Level | 1.6 | 1.7 | - | - | - | - | - | - |   | I  | -  | -  |

**Pre-requisites:** 1.Differentiation of function.

2. Integration of function.

3. Basic Probability theory.

#### Contents:

#### Unit-I

**Calculus of complex functions**: Review of function of a complex variable, limits, continuity, and differentiability. Analytic functions: Cauchy-Riemann equations in Cartesian and polar forms. Construction of analytic functions: Milne-Thomson method-Problems. **6L + 1T** 

#### Unit-II

**Conformal transformations**: Introduction. Discussion of transformations:  $w = e^{z}$ ;  $w = z^{2}$ ,  $w = z + \frac{1}{z}$ ,  $z \neq o$ ) Bilinear transformations- Problems.

Complex integration: Line integral of a complex function, Cauchy's theorem and<br/>Cauchy's Integral theorem.7L + 1T

#### Unit-III

**Statistical Methods**: Correlation and Lines of regression-problems - Fitting the curves of the form y = ax + b;  $y = ax^2 + bx + c$ ;  $y = ax^b$  by the method of least squares. **7L + 1T** 

#### **Unit-IV**

**Probability Distributions**: Random variables (discrete and continuous), probability mass/density functions. Binomial, Poisson, exponential and normal distributions-problems (No derivation for mean and standard deviation)-Illustrative examples.

7L + 1T

#### Unit-V

**Joint probability distribution:** Joint Probability distribution for two discrete random variables, expectation and covariance.

**Markov chains** – Introduction, probability vectors, Stochastic Matrices, Fixed points and Regular stochastic matrices, Markov chains, higher transition probabilities, stationary distribution of regular Markov chains and absorbing states. **7L + 1T** 

#### Reference Books:

- 1. **B.S. Grewal**: Higher Engineering Mathematics, Khanna Publishers, 44<sup>th</sup> Ed., 2017.
- 2. **E. Kreyszig**: Advanced Engineering Mathematics, John Wiley & Sons, 10th Ed.(Reprint), 2016.
- 3. **Peter V.O'Neil**: Advanced Engineering Mathematics, International students edition, 2011.

4.**Kishor S. Trivedi**: Probabilty& Statistics with Reliabilty,Queuing, and Computer Science Applications,Prentice-Hall of India,2005.

# 21UCSM400 Engineering Mathematics – IV (2-2-0) 3

#### Contact Hours: 39

**Course Learning Objectives (CLOs):** This course focuses on the following learning perspectives:

- To have an insight into Fourier series, Fourier transforms, Difference equations and Z-transforms.
- Apply discrete and continuous probability distributions in analyzing the probability models arising in engineering field.

## Course Outcomes (COs):

| Descr          | iption of the Course Outcome:  | Mapping to               | POs(1-12) /<br>16)    | / PSOs (13-         |
|----------------|--|--------------------------|-----------------------|---------------------|
| At the able to | end of the course the student will be<br>o:  | Substantial<br>Level (3) | Moderate<br>Level (2) | Slight<br>Level (1) |
| CO-1           | <b>Express</b> periodic function as a Fourier series and <b>obtain</b> the various harmonics of the Fourier series expansion for the given numerical data.                   | -                        | -                     | 1                   |
| CO-2           | <b>Transform</b> the given function using<br>Fourier transforms depending on the<br>nature of engineering applications.<br>Solve difference equations using Z-<br>transform. | -                        | -                     | 1                   |
| CO-3           | Make <b>Use</b> of the correlation and regression analysis to fit a suitable mathematical model for the statistical data.  | -                        | 1,2                   | -                   |
| CO-4           | <b>Apply</b> discrete and continuous probability distributions in analyzing the probability models arising in engineering field.   | -                        | 1,2                   | -                   |
| CO-5           | Estimate the correlation, covariance   | -                        | 1,2                   | -                   |

| using joint probability distributions.  |
|---|
| Also use student's t-distribution, Chi- |
| square distribution as a test           |
| of goodness of it.                      |

**Pre-requisites:(**1) Differentiation of function.

- (2) Integration of function.
- (3) Basic Probability theory.
- (4) Statistical averages

| POs/PSOs         | 1   | 2   | 3 | 4   | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13  | 14 | 15  | 16 |
|------------------|-----|-----|---|-----|---|---|---|---|---|----|----|----|-----|----|-----|----|
| Mapping<br>Level | 3.0 | 2.0 | - | 1.0 | - | - | - | - | - | -  | -  | -  | 1.0 | -  | 1.0 | -  |

#### Contents:

#### Unit-I

**Fourier Series:** Periodic functions, Dirichlet's condition, Fourier series of periodic functions of period 2 and arbitrary period. Half-range Fourier series, Practical harmonic analysis, Examples from engineering field. **7L + 1T** 

#### Unit-II

**Fourier Transforms:** Infinite Fourier transforms, Fourier sine and cosine transforms, Inverse Fourier transforms, Simple problems.

**Z-Transforms and Difference equations:** Z-transform – definition, Standard Z – transforms, Damping and shifting rules, Initial value and Final value theorems (without proof) with problems, Inverse Z-transform, Simple Problems, Difference equations – Basic definition, Application of Z-transform to solve Difference equation. 7L + 1T

#### Unit-III

**Statistical Methods:** Correlation and regression-Karl Pearson's coefficient of correlation and rank correlation-problems. Regression analysis- lines of regression– problems.

**Curve Fitting:** Curve fitting by the method of least squares- fitting the curves of the form= ax + b;  $y = ax^2 + bx + c$ ;  $y = ax^b$ .7L + 1T

#### Unit-IV

**Probability Distributions:** Review of basic probability theory, Random variables (discrete and continuous), probability mass/density functions. Binomial, Poisson, exponential and normal distributions- problems (No derivation for mean and standard

deviation)-Illustrative examples. **7L + 1T** 

#### Unit-V

**Joint probability distribution:** Joint Probability distribution for two discrete random variables, expectation and covariance.

**Sampling Theory:** Introduction to sampling distributions, standard error, Type-I and Type-II errors. Test of hypothesis for means, student's t-distribution, Chi-square distribution as a test of goodness of fit. **6L + 1T** 

#### **Reference Books:**

- 1) E. Kreyszig: Advanced Engineering Mathematics, John Wiley & Sons, 10th Ed.(Reprint) 2016.
- 2) B.S. Grewal: Higher Engineering Mathematics, Khanna Publishers, 44th Ed., 2017.
- 3) Srimanta Pal et al: Engineering Mathematics, Oxford University Press, 3rd Edition, 2016.

21UECM400

#### **Engineering Mathematics – IV**

(2-2-0)3

**Contact Hours: 39** 

#### **Course Learning Objectives (CLOs):**

To provide an insight into curvilinear coordinates system. Study statistical methods, probability distribution and application of probability distributions in Engineering.

#### **Course Outcomes (Cos):**

| Descri | ption of the Course Outcome: At the  | Mapping to Pos(1-12)/PSOs(13,14) |           |          |  |  |  |  |
|--------|--|----------------------------------|-----------|----------|--|--|--|--|
| end of | the course the student will be able to   | Substantial                      | Moderate  | Slight   |  |  |  |  |
|        |  | Level (3)                        | Level (2) | Level(1) |  |  |  |  |
| CO-1   | <b>Understand</b> the significance of vectors and solve problems in various co-ordinate systems.                                 | 1                                | 2         |          |  |  |  |  |
| CO-2   | <b>Use</b> correlation and regression analysis to fit a suitable mathematical model for the statistical data.                    |                                  | 1,2       |          |  |  |  |  |
| CO-3   | <b>Apply</b> discrete and continuous probability distributions in analyzing the probability models arising in engineering field. |                                  | 1,2       |          |  |  |  |  |
| CO-4   | Recite Markov chains and describe stochastic process.  |                                  | 1,2       |          |  |  |  |  |
| CO-5   | Determine Type-I and Type-II errors<br>and test for goodness of fit using<br>different methods.                                  |                                  |           |          |  |  |  |  |

| Pos/PSOs         | 1   | 2 | 3 | 4 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|------------------|-----|---|---|---|---|---|---|---|----|----|----|----|----|
| Mapping<br>Level | 2.2 | 2 | - | - | - | - | - | - | -  | -  | -  | -  | -  |

**Pre-requisites: (1) Differentiatin of function.** 

- (2) Integration of function.
- (3) Basic Probability theory.
- (4) Vector Algebra.

Curvilinear coordinates system:Vector Field, Dot product, Cross product of<br/>vectors, Other coordinate systems: Circular Cylindrical and Spherical coordinate<br/>systems. Laplace's and Poisson's equations.7L + 1T

#### Unit-II

**Statistical Methods:** Correlation and regression, Karl Pearson's coefficient of correlation and rank correlation, problems. Regression analysis, lines of regression, problems.

**Curve Fitting:** Curve fitting by the method of least squares- fitting the curves of the form = ax + b;  $y = ax^2 + bx + c$ ;  $y = ax^b$ . **Curve Fitting:** bx + b;  $y = ax^2 + bx + c$ ;  $y = ax^b$ . **Curve Fitting:** bx + c;  $y = ax^b$ . **Curve Fitting:** bx + c;  $y = ax^b$ . **Curve Fitting:** bx + c;  $y = ax^b$ . **Curve Fitting:** bx + c;  $y = ax^b$ . **Curve Fitting:** bx + c;  $y = ax^b$ . **Curve Fitting:** bx + c;  $y = ax^b$ . **Curve Fitting:** bx + c; bx + c;  $y = ax^b$ . **Curve Fitting:** bx + c; bx + c

Probability Distributions: Review of basic probability theory, Random variables (discrete and continuous), probability mass/density functions – Uniform, Binomial, Poisson, exponential and normal (Gaussian) distributions, problems (No derivation for mean and standard deviation) - Illustrative examples, Distribution of several random variables.

#### Unit-IV

**Joint probability distributions:** Joint Probability distribution for two discrete random variables, expectation and covariance.

**Markov chains** – Introduction, probability vectors, Stochastic Matrices, Fixed points and Regular stochastic matrices, Markov chains, higher transition probabilities, stationary distribution of regular Markov chains and absorbing states. **7L + 1T**.

#### Unit-V

**Sampling Theory:** Introduction to sampling, estimations of parameters, Confidence intervals, Testing of Hypotheses, Decisions, Standard error, Type-I and Type-II errors, Test of hypothesis for means, student's t-distribution, Chisquare distribution as a test of goodness of fit. **7L + 1T** 

#### Reference Books:

1. ErwinKreyszig: Advanced Engineering Mathematics, John Wiley & Sons 10<sup>th</sup>edition, 2016.

2. B. S. Grewal: Higher Engineering Mathematics, KhannaPublishers,

44<sup>th</sup>edition, 2017.

3. Hayt& Buck, "Engineering Electromagnetics", Tata McGraw-Hill, 8<sup>th</sup> edition, 2010.

4. Edminister, "Electromagnetics", Schaum Outline Series, McGraw Hill, 2<sup>nd</sup> edition, 2006.

#### 21UISM400 Engineering Mathematics-IV (2-2-0)3

#### **Contact Hours:39**

#### **Course Learning Objectives (CLOs):**

To visualize combination, spaces, rotation, reflection and projection of vectors. To compute orthogonal vectors, Eigen values to solve differential and difference equation. Obtain least square solution to solve system of equations.

#### Course Outcomes (COs):

| Descri          | ption of the Course Outcome:   | Mapping to PSO (1 to 2)     | POs(1 t                  | o 12)/                 |
|-----------------|--|-----------------------------|--------------------------|------------------------|
| At the able to: | end of the course the student will be  | Substantial<br>Level<br>(3) | Moderate<br>Level<br>(2) | Slight<br>Level<br>(1) |
| CO-1            | Describe the concept of vector spaces, subspaces, basis, dimension and their properties.   |                             |                          | 1,2                    |
| CO-2            | Explain various matrix transformation<br>such as linear transformation,<br>orthogonal transformation and<br>similarity transformation.         |                             |                          | 1,2                    |
| CO-3            | Illustrate the concepts of symmetric matrices and quadratic forms.   |                             |                          | 1,2                    |
| CO-4            | Apply characteristic polynomials to<br>compute Eigen values and Eigen<br>vectors and use Eigen spaces of<br>matrix to diagonalizable a matrix. |                             |                          | 1,2                    |
| CO-5            | Apply the concepts of inner products to matrix decomposition.  |                             |                          | 1,2                    |

| PO's             | PO1 | PO2 | PO3 | РО<br>4 | РО<br>5 | РО<br>6 | РО<br>7 | РО<br>8 | РО<br>9 | РО<br>10 | РО<br>11 | PO<br>12 | PSO<br>1 | PSO<br>2 |
|------------------|-----|-----|-----|---------|---------|---------|---------|---------|---------|----------|----------|----------|----------|----------|
| Mapping<br>Level | 1.0 | 1.0 | -   | -       | -       | -       | -       | -       | -       | -        | -        | -        | -        | -        |

**Pre-requisites:** 1. Properties of determinants 2. Algebra of Matrices

#### Contents:

### UNIT-I

VECTOR SPACES- Subspaces, Linear Combinations, Linear Spans, row space and column space of a Matrix, Linear Dependence and Independence, Basis and Dimension, Coordinates.
6L+1T

#### UNIT-II

**LINEAR TRANSFORMATIONS:** Introduction, Linear Mappings, Geometric linear transformation of, Kernel and Image of a linear transformations, Matrix representation of linear transformations, Rank-Nullity Theorem (No proof), Singular and Nonsingular linear transformations, Invertible linear transformations.

7L+1T

#### UNIT-III

**SYMMETRIC MATRICES AND QUADRATIC FORMS**: Diagonalization of real symmetric matrices, Orthogonal diagonalization of real symmetric matrices, quadratic forms and its classifications, Singular value decomposition.**7L+1T** 

#### **UNIT-IV**

**EIGEN VALUES AND EIGENVECTORS:** Introduction, Polynomials of Matrices, Characteristic polynomial, Cayley-Hamilton Theorem, eigenvalues and eigenvectors, eigen spaces of a linear transformation, Diagonalization, Minimal Polynomial, Characteristic and Minimal Polynomials of Block Matrices, Jordan Canonical form, Solving differential equations in Fundamental form.**7L+1T** 

#### UNIT-V

**INNER PRODUCT SPACES**: Inner product, inner product spaces, length and orthogonality, orthogonal sets and Bases, projections, Gram-Schmidt process, QR-factorization, least squares problem and least square error. **7L+1T** 

#### **Reference Books:**

- 1) Linear Algebra and its applications, David C. lay, Steven R. lay, Judi J Mc. Donald, 5<sup>th</sup> edition, 2015, Pearson Education.
- 2) Linear Algebra and its applications, Gilbert Strang, 4<sup>th</sup> edition, 2005, Brooks Cole.